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# Learning with Temporal Point Processes

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## Abstract

In recent years, there has been an increasing number of machine learning models, inference methods and control algorithms using temporal point processes. They have been particularly popular for understanding, predicting, and enhancing the functioning of social and information systems, where they have achieved unprecedented performance. This tutorial aims to introduce the machine learning community at large to temporal point processes. In the first of the tutorial, we will first provide an introduction to the basic theory of temporal point processes, then revisit several types of points processes, and finally introduce advanced concepts such as marks and dynamical systems with jumps. In the second and third parts of the tutorial, we will explain how temporal point processes have been used in developing a variety of recent machine learning models and control algorithms, respectively. Therein, we will revisit recent advances related to, *e.g.*, deep learning, Bayesian nonparametrics, causality, stochastic optimal control and reinforcement learning. In each of the above parts, we will highlight open problems and future research to facilitate further research in temporal point processes within the machine learning community.

## 1. Outline of the tutorial

The 2-hour tutorial will be divided into three parts. The first part will give a brief introduction to the theory of temporal point processes, starting from the basics. The second part will go through a variety of machine learning models and efficient inference algorithms which utilize temporal point processes in a wide range of application domains. The third part will introduce several recent control algorithms

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control using temporal point processes and their connections to dynamical systems, stochastic optimal control and reinforcement learning.

### 1.1. Introduction (30 minutes)

We will first provide an introduction to the basic theory of temporal point processes (Daley & Vere-Jones, 2007), starting from the type of data they are a natural fit for. Building on the basic theory, we will revisit several types of *canonical* point processes, such as Poisson processes, self-exciting point processes (*e.g.*, Hawkes processes (Hawkes, 1971)) or survival processes, each especially well fitted for a set of specific application domains. Then, we will present the notion of marks (or marked temporal point processes), a powerful mechanism which have been used to design complex models with random variables whose distribution depend on temporal point processes. Finally, we will introduce an alternative representation of marked temporal point processes as dynamical systems with jumps, which have been recently used to develop highly expressive models as well as sophisticated control algorithms.

### 1.2. Models (60 minutes)

We will elaborate on several specific examples of temporal point process models and efficient inference algorithms proposed in recent years, which leverage the concepts introduced in the first part of the tutorial as well as recent advances in machine learning.

More specifically, in terms of methodology, we will introduce the Dirichlet-Hawkes process and the hierarchical Dirichlet-Hawkes process (Du et al., 2015; Mavroforakis et al., 2017; Xu & Zha, 2017), recurrent temporal point processes (Dai et al., 2016; Mei & Eisner, 2017; Jing & Smola, 2017; Trivedi et al., 2017), deep generative models of temporal point processes (Xiao et al., 2017a; 2018), models based on dynamical systems and stochastic differential equations (SDEs) with jumps (De et al., 2016; Lee et al., 2016; Farajtabar et al., 2017a), and causal inference with temporal point processes (Li et al., 2017; Xu et al., 2016; Kusmierczyk & Gomez-Rodriguez, 2018).

In terms of applications, we will provide a wide variety of examples in social and information networks (Gomez-Rodriguez et al., 2011; Du et al., 2012; Iwata et al., 2013;

Du et al., 2015; De et al., 2016; Farajtabar et al., 2017a; Rizoïu et al., 2017; Mei & Eisner, 2017; Wang et al., 2017c;d), knowledge representation (Mavroforakis et al., 2017; Tabibian et al., 2017b; Trivedi et al., 2017), recommendation systems (Dai et al., 2016; Wang et al., 2016; Jing & Smola, 2017), human mobility (Jankowiak & Gomez-Rodriguez, 2017; Wang et al., 2017a), financial applications (Ahab et al., 2017; Linderman & Adams, 2014), crime prediction (Egesdal et al., 2010; Mohler et al., 2013) health (Alaa et al., 2017; Rizoïu et al., 2018; Xiao et al., 2017b), and biology (Gupta et al., 2017).

### 1.3. Control (30 minutes)

We will first elaborate on the key innovation shared by most recent control algorithms leveraging temporal point processes—the control policy is an intensity function, often stochastic, which characterizes a temporal point process used as control signal. Then, we will present a variety of offline and online control algorithms based on, *e.g.*, convex optimization (Farajtabar et al., 2014; 2016), stochastic optimal control of dynamical systems with jumps (Karimi et al., 2016; Tabibian et al., 2017a; Kim et al., 2018; Zarezade et al., 2018; Wang et al., 2017b), and reinforcement learning (Farajtabar et al., 2017b). Finally, we will point out open problems and directions for future work.

## 2. Past tutorials on the topic

In recent years, we presented three closely related tutorials in top conferences in data mining, the Web, and AI:

- (a) “Diffusion in Social and Information Networks: Problems, Models and Machine Learning Methods” at KDD ’15. The tutorial slides are available at <http://learning.mpi-sws.org/kdd-2015-tutorial/><sup>1</sup>.
- (b) “Diffusion in Social and Information Networks: Research Problems, Probabilistic Models and Machine Learning Methods” at WWW ’15. The tutorial slides are available at <http://learning.mpi-sws.org/www-2015-tutorial/>.
- (c) “Machine Learning for Dynamic Social Network Analysis” at IJCAI ’17. The tutorial slides are available at <http://learning.mpi-sws.org/ijcai-2017-tutorial/>.

However, our tutorial will differ from the above in two key aspects, which we believe will raise the interest of the

<sup>1</sup>The video recordings are available at [https://youtu.be/jCIDFbMjz3g?list=PLn0nrSd4xjjaNzvUtxHzU64xTz4Y\\_XNK9](https://youtu.be/jCIDFbMjz3g?list=PLn0nrSd4xjjaNzvUtxHzU64xTz4Y_XNK9) (first part) and [https://youtu.be/TMnUp-87cpk?list=PLn0nrSd4xjjaNzvUtxHzU64xTz4Y\\_XNK9](https://youtu.be/TMnUp-87cpk?list=PLn0nrSd4xjjaNzvUtxHzU64xTz4Y_XNK9) (second part).

machine learning community at large in temporal point processes. First, it will highlight connections between recent models and methods based on temporal point process and other techniques in the machine learning literature, *e.g.*, Bayesian nonparametrics, deep neural networks, dynamical systems, stochastic optimal control, and reinforcement learning. Second, it will not be restricted to applications in social and information systems.

## 3. Goals

In our tutorial, we aim to provide an in-depth introduction to the theoretical framework of temporal point processes, which underpins a variety of recent machine learning models, inference methods and control algorithms. The participants will learn about the most recent trends as well as open problems and directions for future work.

This tutorial aims to introduce the machine learning community at large to temporal point processes, which have been proven to be very effective in an increasing range of applications but they are not yet very well-known in the community. Our tutorial relates to several areas within the ICML community such as, *e.g.*, probabilistic and graphical models, time series analysis, deep learning, optimal control, reinforcement learning, computational social science, and novel applications in machine learning.

## 4. Target Audience and Prerequisites

This tutorial is meant for a broad audience at ICML, including students and researchers specifically interested in temporal point process models and machine learning methods in the context of computational social science, social and information networks, and the Web. We expect the tutorial to be well attended, with at least 50-60 researchers

No specific knowledge will be required beyond basic probability and core machine learning methods; the tutorial is self-contained and most of the foundational concepts are introduced during the tutorial.

## 5. Tutors’ bio and expertise

Manuel Gomez Rodriguez will present “Representation” (30 minutes) and “Control” (30 minutes) and Isabel Valera will present “Models” (60 minutes).

**Manuel Gomez Rodriguez** is a tenure-track independent research group leader at the Max Planck for Software Systems. Manuel develops machine learning and large-scale data mining methods for the analysis, modeling, and control of large real-world social and information systems. He is particularly interested in problems motivated by the Web and social media and has received several recognitions

for his research, including an Outstanding Paper Award at NIPS'13 and Best Research Paper Honorable Mentions at KDD'10 and WWW'17. Manuel holds a PhD in Electrical Engineering from Stanford University and a BS in Electrical Engineering from Carlos III University in Madrid (Spain), and has been a Barrie de la Maza Fellow and a Caja Madrid Fellow.

Isabel Valera is TBD.

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